

# Stable population coding for working memory coexists with heterogeneous neural dynamics in prefrontal cortex

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**Working memory (WM) is a cognitive function for temporary maintenance and manipulation of information, which requires conversion of stimulus-driven signals into internal representations that are maintained across seconds-long mnemonic delays. Within primate prefrontal cortex (PFC), a critical node of the brain's WM network, neurons show stimulus-selective persistent activity during WM, but many of them exhibit strong temporal dynamics and heterogeneity, raising the questions of whether, and how, neuronal populations in PFC maintain stable mnemonic representations of stimuli during WM. Here we show that despite complex and heterogeneous temporal dynamics in single-neuron activity, PFC activity is endowed with a population-level coding of the mnemonic stimulus that is stable and robust throughout WM maintenance. We applied population-level analyses to hundreds of recorded single neurons from lateral PFC of monkeys performing two seminal tasks that demand parametric WM: oculomotor delayed response and vibrotactile delayed discrimination. We found that the high-dimensional state space of PFC population activity contains a low-dimensional subspace in which stimulus representations are stable across time during the cue and delay epochs, enabling robust and generalizable decoding compared with time-optimized subspaces. To explore potential mechanisms, we applied these same population-level analyses to theoretical neural circuit models of WM activity. Three previously proposed models failed to capture the key population-level features observed empirically. We propose network connectivity properties, implemented in a linear network model, which can underlie these features. This work uncovers stable population-level WM representations in PFC, despite strong temporal neural dynamics, thereby providing insights into neural circuit mechanisms supporting WM.**

working memory | prefrontal cortex | population coding

The neuronal basis of working memory (WM) in prefrontal cortex (PFC) has been studied for decades through single-neuron recordings from monkeys performing tasks in which a transient sensory stimulus must be held in WM across a seconds-long delay to guide a future response. These studies discovered that a key neural correlate of WM in PFC is stimulus-selective persistent activity, i.e., stable elevated firing rates in a subset of neurons, that spans the delay (1). These neurophysiological findings have grounded a leading hypothesis that WM is supported by stable persistent activity patterns in PFC that bridge the gap between stimulus and response epochs. Because the timescales of WM maintenance (several seconds) are longer than typical timescales of neuronal and synaptic integration (~10–100 ms), mechanisms at the level of neural circuits may be critical for generating WM activity in PFC (2). A leading theoretical framework proposes that PFC circuits subserves WM maintenance through

dynamical attractors, i.e., stable fixed points in network activity, generated by strong recurrent connectivity (3, 4).

Recent neurophysiological studies have called into question whether WM activity in PFC can be appropriately understood in terms of persistent activity and attractor dynamics. These studies highlight the high degree of heterogeneity and strong temporal dynamics in single-neuron responses during WM (5, 6), rather than temporally constant activity patterns. Because only a small proportion of WM-related PFC neurons show well-tuned, stable persistent activity, attractor dynamics may not be the dominant form of WM coding. Researchers have emphasized alternative forms of population coding, specifically dynamic coding, in which the mnemonic representation shifts over time during WM maintenance (7, 8). In turn, such observations have motivated theoretical proposals for alternative neural circuit mechanisms for WM that produce dynamical and heterogeneous activity (9, 10).

These studies centralize a tension between temporal dynamics and stable coding of stimulus features during WM maintenance. In high-dimensional state spaces of network activity, however, it is possible for heterogeneous neuronal dynamics to coexist with a stable population coding for WM within a specific subspace

## Significance

**Working memory (WM) is a core cognitive function thought to rely on persistent activity patterns in populations of neurons in prefrontal cortex (PFC), yet the neural circuit mechanisms remain unknown. Single-neuron activity in PFC during WM is heterogeneous and strongly dynamic, raising questions about the stability of neural WM representations. Here, we analyzed WM activity across large populations of neurons in PFC. We found that despite strong temporal dynamics, there is a population-level representation of the remembered stimulus feature that is maintained stably in time during WM. Furthermore, these population-level analyses distinguish mechanisms proposed by theoretical models. These findings inform our fundamental understanding of circuit mechanisms underlying WM, which may guide development of treatments for WM impairment in brain disorders.**

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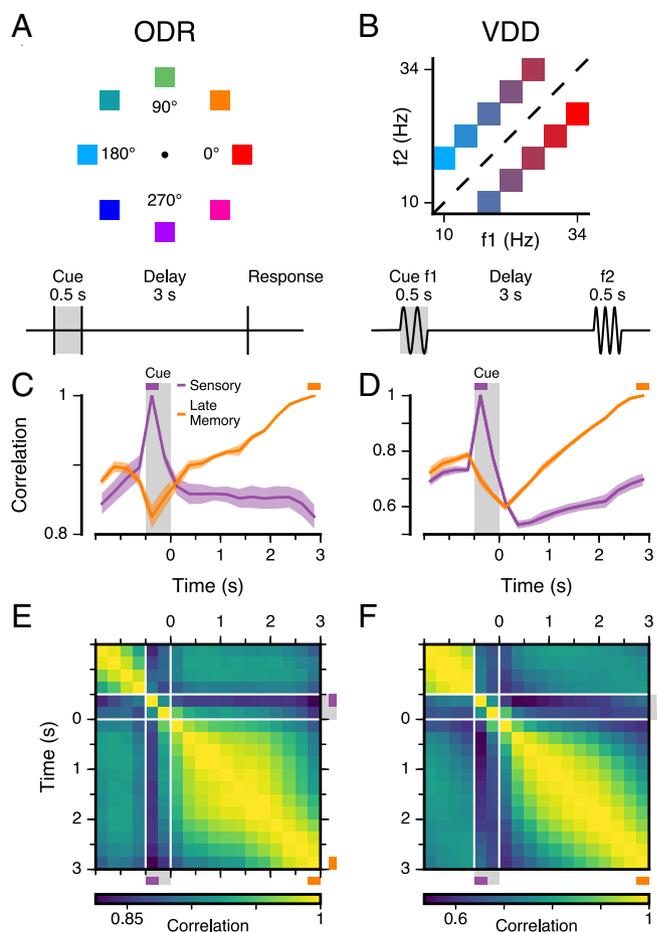
(11). Whether dynamic activity in PFC supports a robust stable population coding for WM remains unclear. Furthermore, dynamic coding raises the challenge of how WM information in PFC can be robustly read out through plausible neurobiological mechanisms, because a subspace corresponds to a set of readout weights (12).

To investigate these issues, we applied population-level analyses to two large datasets of single-neuron spike trains recorded in PFC, from two seminal WM tasks: the oculomotor delayed response (ODR) task (13, 14) and the vibrotactile delayed discrimination (VDD) task (15). In both tasks, PFC populations exhibit strong temporal dynamics during WM, yet there exists a subspace, identifiable via principal component analysis (PCA), in which mnemonic representations are coded stably in time. This mnemonic subspace supports decoding throughout WM, performing comparably to dynamic coding subspaces. We found that population measures dissociate among mechanisms in three previously proposed WM circuit models. Key features of the PFC data are not captured by these three models, yet they are by a simple subspace attractor model. Taken together, our findings demonstrate a stable and robust population coding for WM in PFC and pose constraints for circuit mechanisms supporting WM.

## Results

**Tasks and Datasets.** The ODR and VDD tasks share common features, facilitating comparison across datasets. Both tasks demand parametric WM of an analog stimulus variable: visuospatial angle for ODR and vibrotactile frequency for VDD (Fig. 1 *A* and *B*). Both tasks have a 0.5-s cue epoch followed by a 3-s delay epoch, which is relatively long and allows characterization of time-varying WM representations. The tasks also contrast in several features, allowing us to test the generality of our findings. They differ in stimulus modality (visual for ODR vs. somatosensory for VDD), role of WM in guiding behavioral response (veridical report of location for ODR vs. binary discrimination for VDD), and prototypical stimulus tuning curves of single PFC neurons (bell shaped for ODR vs. monotonic for VDD). Each dataset, collected by a different laboratory, contains spike trains from hundreds of single neurons (645 for ODR; 479 for VDD) recorded from the lateral PFC of two macaque monkeys (14, 15). To minimize bias in characterizing population activity, neurons were not preselected for tuning properties. We used a pseudopopulation approach to study the state-space dynamics of population activity (8, 12, 16, 17), rather than the properties of the heterogeneous individual neurons (Figs. S1 and S2). The activity of  $N$  neurons corresponds to a vector in an  $N$ -dimensional space, with each dimension representing the firing rate of one neuron. The time-varying population activity for each stimulus condition thereby corresponds to a trajectory within this space.

**Population Dynamics.** We first examined the dynamics of population activity during WM by characterizing the similarity of activity patterns between two timepoints. We calculated the correlation, across neurons, between the population state at one timepoint and the state at another timepoint, within a stimulus condition (18). Fig. 1 *C* and *D* shows the time course of this similarity for two reference timepoints: a “sensory” state during the cue epoch and a “late memory” state at the end of the delay epoch. Fig. 1 *E* and *F* shows the population correlation across all timepoints. For both datasets, WM activity patterns in PFC exhibit strong temporal dynamics with the population state changing strongly throughout the cue and delay epochs. The strength of these dynamics can be observed in the late memory trace (Fig. 1 *C* and *D*): The correlation for early in the delay is as low as it is for the foreperiod. These temporal dynamics at the population level are consistent with prior characterizations



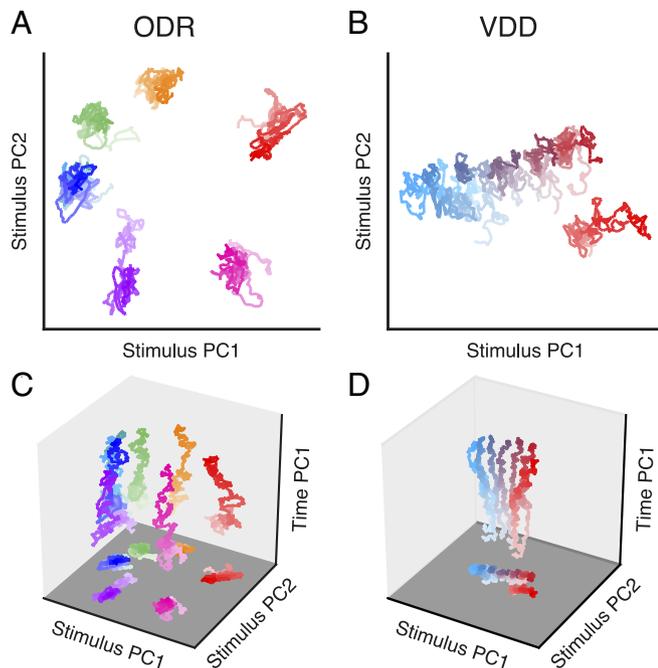
**Fig. 1.** WM tasks and PFC population dynamics. (*A*) In the ODR task, the subject fixates on a central point, and a visuospatial cue of variable spatial angle is presented for 0.5 s, followed by a 3-s mnemonic delay. After the delay, the subject makes a saccadic eye movement to the remembered location (14). (*B*) In the VDD task, the subject receives a 0.5-s vibrotactile stimulus of variable mechanical frequency (cue,  $f_1$ ) to the finger, followed by a 3-s mnemonic delay. After the delay, a second stimulus ( $f_2$ ) is presented and the subject reports, by level release, which stimulus had a higher frequency (15). (*C* and *D*) Correlation between population states as a function of time, within the same stimulus condition. The sensory state is defined by the first 0.25 s of the cue epoch and the late memory state by the last 0.25 s of the delay epoch. Colored shaded regions mark SEM. (*E* and *F*) Correlation between the population states at different timepoints (i.e., time-lagged autocorrelation). The correlation between states is generally high due to a broad distribution of overall firing rates across neurons (Fig. S2). The traces in *C* and *D* are slices along the corresponding timepoint.

of delay dynamics at the single-neuron level (5, 6). We note that trial averaging could obscure dynamics (e.g., oscillations) that are not phase locked to task timing.

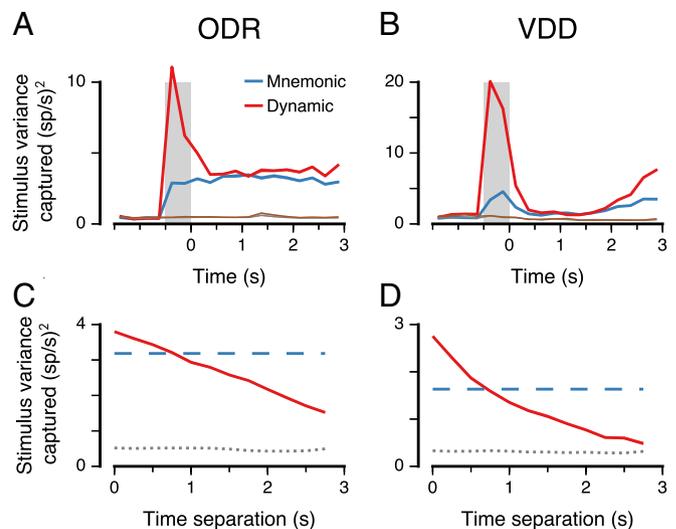
**Stable Coding in a Mnemonic Subspace.** Are these strong population dynamics compatible with stable coding for WM? In the state-space framework, stable mnemonic coding corresponds to a fixed subspace within which the neural trajectories during WM are relatively time invariant and separable across stimulus conditions. To test this hypothesis, we sought to define and characterize a mnemonic coding subspace. There are a variety of dimensionality reduction methods to define candidate coding subspaces. Motivated by the neurobiological relevance of a mnemonic subspace, which may provide representations for downstream readout of WM, we sought to define a subspace that can be plausibly learned for readout via known forms of synaptic

plasticity. There is an established theoretical literature linking Hebbian learning to dimensionality reduction via PCA (19–21). We therefore applied PCA to the time-averaged delay activity across stimulus conditions (*SI Text*) (Fig. S3). The leading  $k$  principal axes, ranked by variance captured, define a  $k$ -dimensional linear subspace, which we denote the mnemonic subspace, which lies closest on average to the datapoints. Because this subspace is defined by time-averaged activity, our approach does not explicitly use timing information (as in ref. 16). A primary rationale is that if a subspace is accessible through time-insensitive PCA, then it can potentially be learned neurally through Hebbian plasticity.

Surprisingly, we found that when the neural trajectories are projected into the mnemonic subspace, the resulting delay activity is remarkably stable in time, even though this subspace is not designed to minimize temporal variation (Fig. 2*A* and *B*). Separation and stability of trajectories can be quantified and compared through the across-condition stimulus variance and within-condition time variance (Fig. S4). For ODR, the first two principal components (PCs) of the mnemonic subspace (i.e., the projections of the activity along the corresponding principal axes) largely reflect the horizontal and vertical stimulus dimensions (Fig. 2*A* and Fig. S3*C*). For the leftmost three locations, traces overlap in the PC1–PC2 subspace but are distinguishable in higher PCs (Fig. S3*E* and *F*). This compressed representation of the ipsilateral (left) visual hemifield is expected due to the prominent contralateral bias for coding of visual space in PFC (13, 22). For VDD, the first PC of the mnemonic subspace provides a monotonic, quasi-linear ordering of the cue stimulus fre-



**Fig. 2.** Stable population coding of WM coexists with strong temporal dynamics. (*A* and *B*) Population trajectories during the WM delay epoch projected into the mnemonic subspace, defined via PCA on time-averaged delay activity. Here the  $x$  and  $y$  axes show the first and second principal components (PC1 and PC2) of the subspace. Each trace corresponds to a stimulus condition, colored as in Fig. 1*A* and *B*. The shading of the traces marks the time during the delay, from early (light) to late (dark). (*C* and *D*) Three-dimensional projections, illustrating the strong temporal dynamics coexisting with stable coding in the mnemonic subspace. The  $x$  and  $y$  axes are as in *A* and *B*. The  $z$  axis (time PC1) is an orthogonal axis in the state space that captures time-related activity variance, but does not indicate time explicitly. Within each plot, all axes are scaled equally.



**Fig. 3.** Stimulus variance captured by the mnemonic and dynamic coding subspaces. The mnemonic subspace is defined using delay activity as in Fig. 2. The dynamic subspace is defined from data for each timepoint (0.25 s). The dimensionality of the subspaces is 2 for ODR (*A* and *C*) and 1 for VDD (*B* and *D*), matching the dimensionality of the stimulus feature for each task. (*A* and *B*) Stimulus variance captured for stable mnemonic subspace (blue) and for a dynamic subspace optimized for each timepoint (red). Chance values for the stable (gray) and dynamic (brown) subspaces were calculated by shuffling stimulus trial labels. (*C* and *D*) Generalizability of the dynamic subspace across time. The red curve marks the stimulus variance captured by the dynamic subspace defined at one time for activity at another time separated by a given time separation, averaged across timepoints during the delay. The blue dashed line marks the stimulus variance captured by the mnemonic subspace, averaged across the delay epoch. The gray dotted line marks the mean chance level during the delay. Shaded bands mark SEM.

quency (Fig. 2*B* and Fig. S3*D*). To visualize population temporal dynamics in relation to the mnemonic subspace, we constructed 3D projections. In Fig. 2*C* and *D*, the  $x$  and  $y$  axes show the first two PCs of the mnemonic subspace. The  $z$  axis is an orthogonal axis in the state space that captures a large amount of time variance during the delay. Mnemonic subspace trajectories vary in time more for VDD than for ODR, exhibiting a gradual increase in separation during the delay. As this view shows, WM activity undergoes strong changes over time without interfering with coding that is stable and separable within the mnemonic subspace.

**Stable and Dynamic Coding.** We have shown that the PCA-defined mnemonic subspace captures a relatively stable stimulus representation throughout the WM delay. However, this subspace may not capture components of the WM representation that are highly dynamic during the delay. In a dynamic coding scenario, a fixed subspace would fail to capture much stimulus variance, because stimulus representations change over time, and a “dynamic” subspace that is reoptimized for each timepoint would capture a much larger amount of stimulus variance. To characterize the relative strengths of stable and dynamic coding, we measured the amount of stimulus variance captured by a given subspace (i.e., the resulting firing-rate variance across stimuli when the population activity, at a given timepoint, is projected into the subspace), for the mnemonic subspace as well as for a dynamic subspace that is redefined for each timepoint by the same PCA method. To allow proper comparison between mnemonic and dynamic subspaces, we applied a split-data approach for cross-validation and used equal amounts of training data (*SI Text*).

We found that the mnemonic and dynamic subspaces capture significantly more stimulus variance than expected by chance for

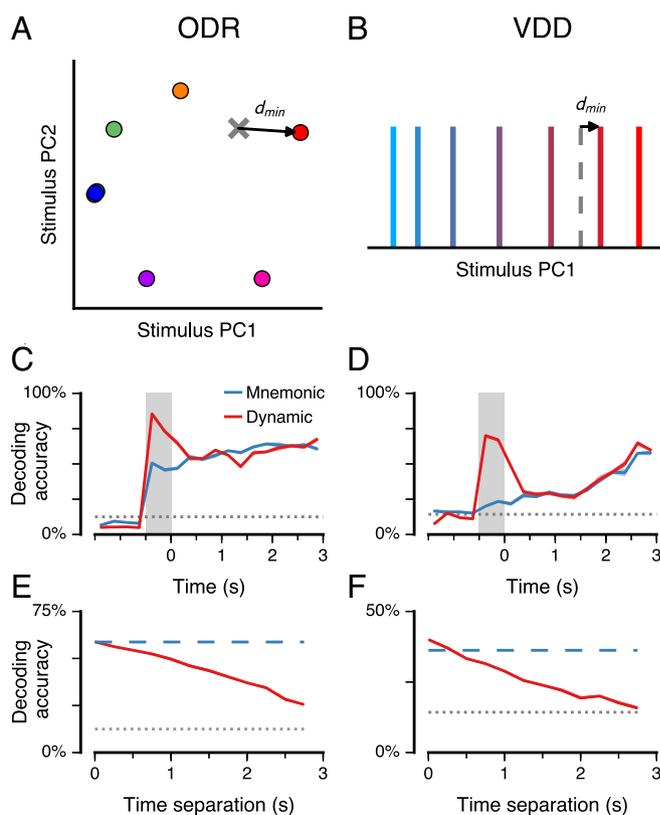
all timepoints across the cue and delay epochs ( $P < 0.01$ ,  $t$  test) (Fig. 3 *A* and *B*). The mnemonic subspace encodes a comparable amount of variance across the cue and delay epochs, even though it was defined using only delay-epoch data, suggesting that mnemonic coding begins early during stimulus presentation. Relative to the mnemonic subspace, the dynamic subspace captures a comparable amount of stimulus variance during the delay, but substantially more during the cue. This suggests a separate sensory representation that is activated during stimulus presentation. For VDD but not ODR, the variance increases substantially toward the end of the delay, due to dynamic coding as well as increased separation within the mnemonic subspace, which could potentially be due to task differences in response type. We tested generalizability of the dynamic subspace by measuring how well the subspace defined at one timepoint captures stimulus variance in activity at a different timepoint. The amount of variance captured decays smoothly with increasing separation between these two timepoints (Fig. 3 *C* and *D* and Fig. S5), reflecting the timescales over which dynamic coding evolves. For zero time separation, the dynamic subspace captures more variance on average than the mnemonic subspace, but for all separations greater than 0.5 s, the mnemonic subspace captures more variance, showing robustness of stable coding in this subspace.

**Decoding.** The above findings do not directly test whether the stimulus can be reliably decoded from neural activity. Even within a fixed subspace, representations could potentially rearrange within the subspace across time. To explicitly quantify decoding accuracy from the mnemonic and dynamic subspaces, we designed a neurobiologically plausible decoder based on the nearest-centroid classifier (*SI Text*). This simple classifier has a straightforward neural interpretation: winner-take-all selection following readout from the low-dimensional linear readout weights defining the subspace. We reserve the spike counts for a given timepoint from a single trial, for leave-one-out cross-validation. We construct decoding subspaces, mnemonic and dynamic, as well as the centroids related to each stimulus condition in those subspaces, using equal amounts of training data from the other trials. The classifier choice is given by the stimulus condition whose centroid is nearest to the test datapoint (Fig. 4 *A* and *B*).

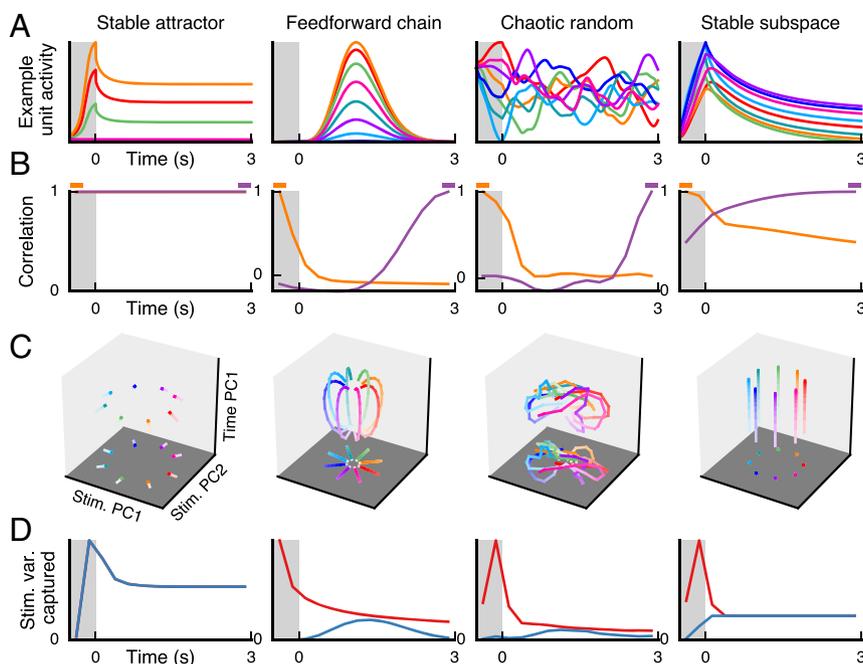
We found that the mnemonic subspace yielded decoding performance that is above chance during the delay epoch and during the cue epoch ( $P < 0.01$ ,  $t$  test), even though the subspace was trained using only delay-epoch data (Fig. 4 *C* and *D* and Fig. S6). Both subspaces produced comparable performance during the delay epoch. Errors in the mnemonic subspace were typically made to similar stimulus conditions (Fig. S6). Relative to mnemonic, the dynamic decoder performed substantially better during the cue and early delay. As with variance captured (Fig. 3*B*), for VDD decoding improves in the late delay. For some timepoints the dynamic decoder performed slightly worse than the mnemonic decoder, potentially due to noisy subspace estimation from limited trials. We tested generalizability across time of the dynamic subspace classifier (Fig. 4 *E* and *F* and Fig. S6) and found a gradual decay in performance with increasing time separation, consistent with prior studies (7, 8). Compared with mnemonic, the dynamic decoder had marginally higher decoding performance at zero time separation, but substantially lower performance when applied to separations greater than 0.5 s.

**Neural Circuit Models.** What implications do these findings have for the neural circuit mechanisms supporting WM activity in PFC? To investigate this, we applied the same population-level analyses to four theoretical models of neural WM circuits. We first analyzed three previously proposed circuit models (*SI Text*). The first model, denoted as a “stable attractor” network, uses

strong recurrent excitation and lateral inhibition to maintain a stimulus-selective persistent activity pattern as a stable fixed point of the network dynamics (3, 23). The second model is denoted as a “feedforward chain” network (9). In contrast to the recurrent excitation in the stable attractor model, this network has a feedforward chain structure of excitatory connections, and information is encoded only transiently in each neuron. In the third model, denoted as a “chaotic random” network, recurrent connections are random but strong, placing the network dynamics in a chaotic regime (10, 24). Stimulus presentation temporarily suppresses chaotic activity, allowing the network to reliably encode the stimulus (25). During the delay, the network activity evolves chaotically from this stimulus-selective point, generating activity patterns that are distinguishable across stimuli but with representations that change over time. We found that none of these models captured key features of WM population coding observed in the PFC datasets (Fig. 5 *A–D*, *Left-most three columns*). The stable attractor model exhibits stable coding in the mnemonic subspace, but not strong temporal dynamics, because network activity is at a fixed point during the delay. In contrast, the feedforward chain and chaotic random



**Fig. 4.** Decoding of stimulus via stable and dynamic coding subspaces. (*A* and *B*) Schematic of the subspace decoder. Activity at a given timepoint for a single trial is projected into the subspace, and the classifier’s winner-take-all readout is the stimulus condition whose centroid is nearest ( $d_{min}$ ). As in Fig. 3, the number of dimensions used for the subspace is 2 for ODR and 1 for VDD. (*C* and *D*) Decoding accuracy over time for the mnemonic (blue) and dynamic (red) coding subspaces. Chance performance for the stable (gray) and dynamic (brown) subspaces was calculated by shuffling stimulus trial labels. (*E* and *F*) Generalizability of the dynamic subspace across time. The red curve marks the stimulus variance captured by the dynamic subspace defined at one time for activity at another time separated by a given time separation, averaged across timepoints during the delay. The blue dashed line marks the stimulus variance captured by the mnemonic subspace, averaged across the delay epoch. The gray dotted line marks chance performance. Shaded bands mark SEM.



**Fig. 5.** Population-level analyses measures distinguish theoretical model network mechanisms for population coding and dynamics. We tested four dynamical circuit models, described in the main text: stable attractor, feedforward chain, chaotic random, and stable subspace. The simulated stimulus features are designed to match the ODR task. (A) Example activity for one neural unit in the network. Each colored trace indicates a different stimulus condition, as for ODR. (B) Correlation of population state as a function of time, as in Fig. 1 C and D. We show the correlation for each timepoint with the sensory (orange) and late memory (purple) states. (C) Delay-activity state-space trajectories, as in Fig. 2 C and D. (D) Stimulus variance captured over time, for mnemonic (blue) and dynamic (red) coding subspaces, as in Fig. 3 A and B.

models exhibit strong temporal dynamics, but both fail to exhibit stable coding in the mnemonic subspace, because WM representations change throughout the delay.

Motivated by our empirical findings, we built a simple circuit model, which we denote a “stable subspace” model, designed on three principles that constrain the recurrent and input connectivity (*SI Text*). First, there is a mnemonic coding subspace in which network dynamics are stable in the absence of stimulus input. Second, the stimulus input pattern should partially align with this coding subspace, activating a representation within the subspace. Third, the noncoding subspace can exhibit temporal dynamics that are orthogonal to the coding subspace. Druckmann and Chklovskii (11) proposed a similar model mechanism. We found that a linear network model with these properties can capture the key observed features of population coding and dynamics (Fig. 5 A–D, *Rightmost column*). It exhibits stable coding in the mnemonic subspace and strong temporal dynamics orthogonal to it. Due to partial alignment of the stimulus input vector with the mnemonic subspace, there is a sensory representation that decays following stimulus removal, whereas the orthogonal mnemonic representation persists (Fig. 5D, *Right*).

## Discussion

**Stable and Dynamic Population Coding.** Prior studies have characterized dynamic WM coding by testing how well a decoder defined at one time generalizes to other times (7, 8). Our findings extend these by showing that dynamic coding during WM can coexist with stable subspace coding that is comparably strong. Our analyses reveal both stable and dynamic components of WM coding, with dynamic components especially strong during the cue and early delay. Comparable decoding performance of the mnemonic subspace during the delay suggests that stable WM coding in the mnemonic subspace is robust and suitable for downstream neural readout of WM signals from PFC. Our findings also shed light on the relationship between sensory

and mnemonic coding in PFC. Prior dynamic coding analyses led to proposals of a sequential transition from a sensory representation during the cue to a mnemonic representation during the delay (8, 18), seemingly in contrast to persistent activity models of WM. Our findings suggest that during cue presentation an activated mnemonic representation coexists with a quasi-orthogonal sensory representation that then decays during the delay while the mnemonic representation stably persists.

**Neural Readout.** Our findings of stable coding in a mnemonic subspace have implications for possible downstream readout of WM information from the PFC and how WM information combines with subsequent input to guide decisions (4). A subspace corresponds to sets of synaptic readout weights to downstream neural systems. In the state–space framework, dynamic WM coding poses challenges for neurobiologically plausible readout of WM information. Purely dynamic coding demands different sets of readout weights at different timepoints; downstream systems would need to measure elapsed time to select the appropriate set of weights. In contrast, stable coding within a fixed subspace corresponds to a fixed, common set of weights that allows readout across time. Fixed decoding weights are especially important when WM signals must be flexibly and robustly read out under changes in delay duration. Both tasks analyzed here used a fixed delay duration and could therefore in principle be implemented using dynamic coding, with readout from a single set of readout weights optimized for the end of the delay, yet the PFC populations nonetheless exhibited robust stable WM coding.

The mnemonic subspace was obtained via PCA on time-averaged delay activity and therefore does not directly take precise timing information into account, a feature that strengthens the neural plausibility of such a subspace being used for WM coding. Theoretical studies have established relationships between dimensionality reduction via PCA and unsupervised learning of readout weights via Hebbian plasticity. There are Hebbian

learning rules through which readout weights to a downstream neural system can extract the principal subspace (19, 20), including via local synaptic plasticity rules (21). These features are in contrast to coding subspaces derived from timing-sensitive dimensionality reduction methods such as difference of covariances (DOC) (16) or demixed PCA (dPCA) (26). DOC and dPCA define a subspace in which coding has maximized temporal stability, by explicitly using timing information to separate stimulus-related from time-related activity variance. For these methods it is unknown how neurobiologically plausible learning rules could extract the coding subspaces. We propose that a downstream circuit can harness neurobiologically plausible synaptic plasticity mechanisms to learn readout of the mnemonic subspace. Furthermore, a low-dimensional coding subspace allows information to be transmitted via sparse projections.

**Neural Circuit Mechanisms.** In addition to their neurobiological relevance, one strength of these subspace analyses is that they can dissociate predictions from circuit models that implement WM maintenance via distinct mechanisms. In contrast, timing-based DOC and dPCA analyses can yield apparently stable coding even for dynamic coding mechanisms, such as the random chaotic network (10). Similarly, although the feedforward chain model functions by a quintessential dynamic coding mechanism, one can construct a subspace in which its WM representations are stable (9). Our findings thereby provide population-level constraints on neural circuit mechanisms supporting WM. In particular, they highlight the need for circuit models that capture both stable coding and temporal dynamics. We developed a proof-of-principle linear network model that captures both stable coding in the mnemonic subspace and strong temporal dynamics orthogonal to it. Druckmann and Chklovskii (11) found that stable subspace

models can incorporate neurobiological constraints such as sparse connectivity and that unsupervised Hebbian learning of recurrent connections can produce a stable coding subspace. Our empirical findings are in line with this theoretical framework and suggest that WM activity in PFC may be supported by such stable-subspace network mechanisms (27). Another direction for future circuit modeling is to compare empirical population data to activity in trained recurrent neural networks, which can lie at an intermediate stage of random and structured connectivity (10).

A primary limitation of our datasets is that they were composed of separately recorded neurons, which is common in pseudopopulation state-space analyses (7, 8, 12, 16, 17). It is an open question how correlated single-trial fluctuations may affect mnemonic subspace coding and single-trial decoding. Future studies using large ensembles of simultaneously recorded neurons and single-trial analyses can inform these issues (28, 29). Simultaneous recordings could also test for transient dynamics that are not locked to task timing, as well as test theoretical model predictions for correlated fluctuations within specific coding subspaces (30).

## Materials and Methods

Methods for analyses and models are provided in *SI Text*. Details of both datasets have been previously reported (14, 15). All experimental methods met standards of the US National Institutes of Health and were approved by the relevant institutional animal care and use committees at Yale University and Universidad Nacional Autónoma de México.

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